

# Optimal Control for Battery Storage Using Nonlinear Models

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# Outline

- 1 Introduction
- 2 Optimal charging control using linear and nonlinear models
- 3 Case study
- 4 Conclusion and future work



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# Background

## Grid applications:

- Energy arbitrage
- Balancing service
- Capacity value
- Distribution system upgrade deferral
- Outage mitigation

## Customer-side applications:

- Energy charge reduction
- Demand charge reduction



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# Motivation

- Optimal control is desired in order to best utilize the limited power and energy capacity of BSS
- Look-ahead optimization is required to capture interdependent operation over time
- Fixed power rating and constant round-trip or one-way efficiencies are used in existing optimal scheduling methods
  - ▶ inaccurate economic assessment results
  - ▶ infeasible operating schedule



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# Optimal scheduling with linear battery model

$$\mathbf{P}_1 : \max_{p_k, p_k^{\text{batt}}, s_k, \Delta s_k} \sum_{k=1}^K \lambda_k p_k$$

subject to:

Charging/discharging limit:  $-p_{\max}^- \leq p_k \leq p_{\max}^+, \quad \forall k = 1, \dots, K$

Rate change of energy in batt.:  $p_k^{\text{batt}} = \begin{cases} p_k / \eta^+ & \text{if } p_k \geq 0 \\ p_k \eta^- & \text{if } p_k < 0 \end{cases}, \quad \forall k = 1, \dots, K$

SOC change:  $\Delta s_k = p_k^{\text{batt}} \Delta T / E_{\max}, \quad \forall k = 1, \dots, K$

Dynamics of SOC:  $s_k = s_{k-1} - \Delta s_k, \quad \forall k = 1, \dots, K$

SOC limits:  $\underline{S}_k \leq s_k \leq \bar{S}_k, \quad \forall k = 1, \dots, K$

# Limitations with existing linear battery model

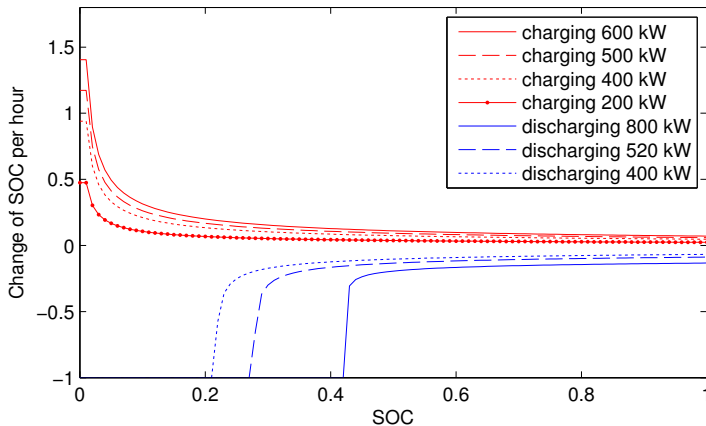
- $[-p_{\min}, p_{\max}]$ : incapable to model varying charging/discharging range
- $E_{\max}$ : inaccurate to represent energy capacity
- $\eta^+, \eta^-$ : difficult to estimate overall efficiency and inaccurate to capture actual losses



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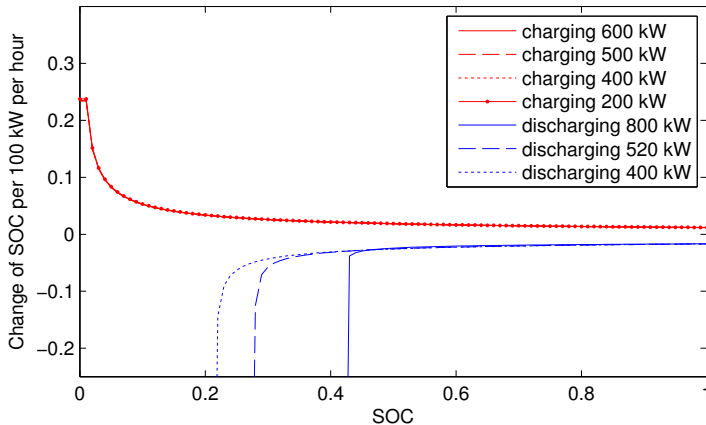
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# Varying power capability and SOC change rate



1 MW/3.2 MWh vanadium redox BSS

## Varying power capability and SOC change rate (cont.)



1 MW/3.2 MWh vanadium redox BSS



# Optimal scheduling with nonlinear battery model

$$\mathbf{P}_2 : \max_{p_k, s_k, \Delta s_k} \sum_{k=1}^K \lambda_k p_k$$

subject to:

Charging/discharging limit:  $p_k \in \mathcal{P}_{s_k}, \quad \forall k = 1, \dots, K$

SOC change:  $\Delta s_k = f(p_k, s_k), \quad \forall k = 1, \dots, K$

Dynamics of SOC:  $s_k = s_{k-1} - \Delta s_k, \quad \forall k = 1, \dots, K$

SOC limits:  $\underline{S}_k \leq s_k \leq \bar{S}_k, \quad \forall k = 1, \dots, K$



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# Assumptions and inputs

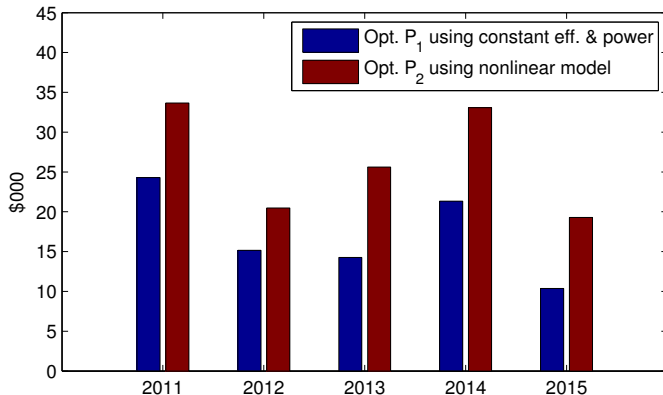
- BSS: 1 MW/3.2 MWh vanadium redox BSS at Turner substation in Pullman in Washington State.
- Applications: energy arbitrage and energy imbalance reduction
- Price: The Mid-Columbia prices from 2011 to 2015



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# Economic performance comparison results



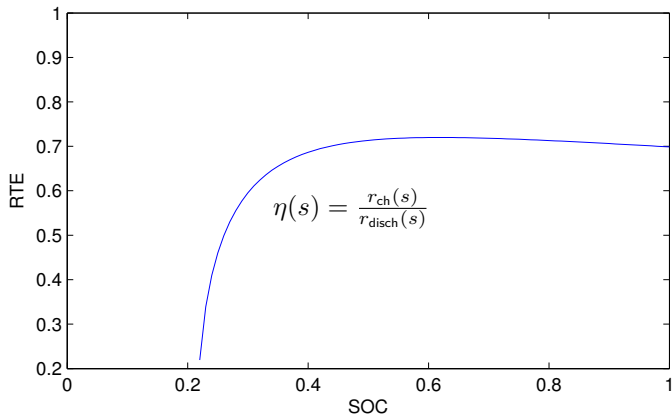
2 MW/6.4 MWh



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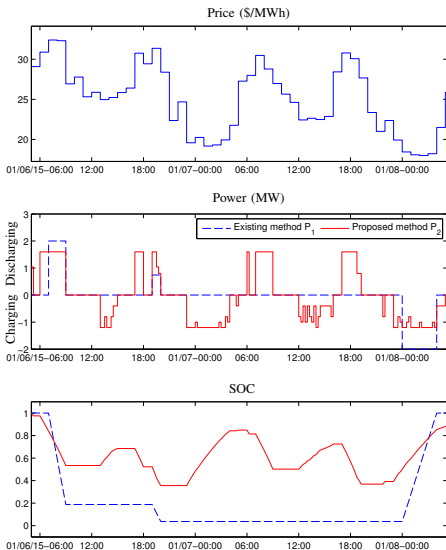
# Varying round-trip efficiency



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# BSS power and SOC



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# Conclusion and future work

## Conclusion:

- Nonlinear BSS model better captures varying charging/discharging power capability and efficiencies.
- Optimal scheduling without accurate nonlinear BSS model could result in significant errors in benefits assessment, and even infeasible operation.

## Future work:

- Apply the proposed method with nonlinear model for other grid and/or customer-side applications.



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Thank you! Questions?

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